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# CROSSWIND COEFFICIENTS OF DIFFUSION <br> AND THEIR 

CORRELATION WITH MICROMETEOROLOGICAL
PARAMETERS

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Suzanne E. DeCarre


# CROSSWIND COEFFICIENTS OF DIFFUSION 

# AND THEIR <br> CORRELATION WITH MICROMETEOROLOGICAL PARAMETERS 

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Submitted in partial fulfillment of the requirements for the degree of MASTER OF SCIENCE IN

METEOROLOGY

United States Naval Postgraduate School Monterey, California

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by
Suzanne E. DeCarre
This work is accepted as fulfilling
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## ABSTRACT

Diffusion measurements were made at the Round Hill Field Station Nebraska in the year 1957. These measurements were used to calculate Ty , the LaGrangian standard deviation in the direction lateral to the mean wind for a series of experimental runs under varying conditions of thermal stability, and horizontal and vertical wind shear. A relationship between Ty and the downwind distance was derived from Sutton's equation for an elevated point source. $\sigma_{y}$ was calculated for the various runs of data and correlated with the crosswind and downwind distances. Correlations were worked out between (i) $\sigma_{y}$ and the standard deviation of the wind angle $\sigma_{A}$ (ii) $\sigma_{y}$ and the contour profile number $p$, and (iii) $\sigma_{y}$ and the stability ratio. A marked correlation was found for $\sigma_{A}$ the azimuth wind variation.

The writer wishes to express her appreciation for the assistance and encouragement given her by Professor Frank L. Martin of the U. S. Naval Postgraduate School in this investigation.


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$C_{x}, C_{y}, C_{z} \quad-\quad$ Generalized diffusion coefficients
co
c
h

Q
r
$R(\xi)$
u
$\sigma_{A}$
$\mathrm{u}_{2}$

- Concentration of aerosol along main axis
- Concentration not along main axis
- Height of the source above the ground
- Source strength
- Correlation coefficient
- Lagrangian autocorrelation coefficient of velocity component of lag
- Wind in the $\mathbf{x}$-direction
- Standard deviation of azimuth wind angle
- Lagrangian deviation along y-axis
- Lagrangian deviation along z-axis
- Wind speed at 2 meters


During the fall of 1957 , a series of diffusion experiments from a steady state point source was conducted at the Round Hill Field Station in Nebraska. The sampling array consisted of three overlapping, independently operated networks at travel distances of 50,100 , and 200 meters. During the experiments, time-mean concentrations for sampling intervals of $.5,3$, and 10 minutes were obtained for each travel distance. A schematic diagram of the field installation is shown by Figure l. The ten-minute network comprised of individual stations located at a height of 1.5 meters and were spaced at 3-degree intervals along 180 degrees of arc: sampling stations for the three-minute network were at a height of 1.5 meters and spaced at 1.5 degree intervals along an arc of 150 degrees.

A sulfur dioxide generator was used to supply the tracer. A point source of strength 100 g per sec was required during conditions of thermal instability while an emission rate of half that amount was sufficient under nighttime thermal conditions of thermal stability. Prior to the start of the experiment, the tracer was permitted to traverse the entire network. The three sampling networks were then turned on simultaneously and each operated for the appropriate length of time. Aspiration of the impingers was provided by ten vacuum tanks. Error introduced into the concentration measurements by the operation of the vacuum system was estimated to be less than five percent.

Meteorological instrumentation included: a cup anemometer and sensitive azimuth vane located at a height of two meters near the source;

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 -  ..... $=1$
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$\frac{1}{2}$
cup anemometers and ventilated thermocouples at heights of $1.5,3,6$, and 12 meters on a portable tower; and for most experiments, five bivanes equipped with heated thermocouple anemometers. The operation of all meteorological instrumentation was controlled by a timer located within the recording truck. A twenty-minute observation period centered on the ten-minute gas sampling period was employed for the meteorological instruments.

2. Theoretical considerations:

Assuming that the mean concentrations within a diffusion cloud are distributed laterally by a two-dimensional normal distribution, Sutton has shown that the steady-state concentration from a point source is given by:
(1) $\bar{C}(x, y, z)=\frac{2 Q}{\Pi \mu \sqrt{y} \sqrt{z}} \cdot d p\left[-\left(\frac{\mu^{2}}{2^{4} y^{2}}+\frac{z^{2}}{z^{2}} \sqrt{2}^{2}\right)\right]$
for a ground source. For an elevated source of height, $h$, the corresponding equation becomes:
 $\left\{\operatorname{edp}\left[\frac{-(z-h)^{2}}{2 \sigma_{z}^{2}}\right]\right.$
$\left.\left.+\exp \frac{-(z+h)}{2 \sigma_{z}{ }^{2}}\right]\right\}$

Sutton's reasoning, in addition to the assumption of the Gaussian distribution of pollutant, is that the concentration shall satisfy the following boundary conditions:
(1). $\bar{c} \rightarrow 0$, as $x, y, z \rightarrow 0$
(2). The downward transport at the earth ${ }^{\circ}$ s surface is zero.

(3). The rate of the total transport of contaminant through any downwind plane is constant and equal to the generation rate at the source.

In this study expression for $\sqrt{y}$ and $\sqrt{2}$ of the form

$$
\nabla y=B x^{b}, f>0
$$

will be sought.
Sutton [ 3 I made certain assumptions regarding the form of the Lagrangian autocorrelation function $R$ ( $y$ ) which relates the $y$-component of velocity with that existing for the same particle at time later. He then obtained:
(4) $\sigma_{y}^{2}=\frac{1}{2} C y^{2} x^{2-w}$
(5) $\sigma_{2}^{2}=\frac{1}{2} C_{2}^{2} x^{2-w}$

Here $C_{y}, C_{z}$ are called the generalized diffusion coefficients. Sutton $\angle 3 \overline{ }$ has obtained formulas $C_{y}, C_{z}$ in terms of the gustiness of the wind. The particular formulas for $C_{y}, C_{z}$ may be found on page 251 of $\overline{3}]$.

The expressions for $\sqrt{y}_{y}^{2}, \sqrt{3}$ of (4), (5) are usually introduced into (1) or (2) at this point. Barad and Hagen $L 1 /$ have tested Sutton ${ }^{\circ}$ s theory using the equation modified in this way. However, the values they found did not agree with $n=2 p / p+1$. Thus in this paper, the more general Sutton theory of Equations (1) and (2) has been used, with the object of determining empirical information regarding $\sigma_{y}$ and $V_{z}$.

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$$





Let $c_{0}$ be the axial concentration at a given downwind distance $x$, and $c_{1}$ the concentration at $(x, y, z)$ where, in the major part of the Round Hill data, $z=1.5$ meters. In order to obtain $\sigma_{y}, \sigma_{z}$ as a function of $x$. the assumption was made that these parameters did not vary over the measuring range lateral to the axis. Therefore, using $c_{o}$ with $y=0$ in Equation (2) we obtain:
(6) $\frac{C_{1}}{C_{0}}=\exp \left(-y^{2} / 2 \sqrt{y^{2}}\right)$

On taking logs of both sides of Equation (6)
(7) $\sqrt{y^{2}}=\frac{y^{2}}{2 \ln (0 / C)}$

This was the main working equation of this paper. A similar procedure will be outlined for $\widetilde{V}_{z}$, although no detailed computations for $\widetilde{V}_{2}$ have been obtained.
3. Research objectives and results:

The first problem of this study was to determine a relationship between $\sqrt{y}$ and the downwind distance $x$ along the mean wind. An equation of the form

$$
\sigma y=B x^{b}, b>0
$$

was tested. Secondly, it was desired to determine the empirical relationship between $\sqrt{y}$ and $x$ and $y$, where $y$ is the distance lateral to the wind axis.

A chemical cloud may be pictured ideally as shown in Figure 2. The data $\angle \underline{2} \overline{\text { p }}$ presented concentrations at only three downwind distances along the axis: at 50 meters, 100 meters and 200 meters. The concentration,


$z$

$$
\begin{aligned}
& r=r a d i u s \text { of } \operatorname{arc} \\
& y=r \sin \theta \\
& x=r \cos \theta
\end{aligned}
$$

Figure 2. Sulfur dioxide cloud from point source

$$
\begin{aligned}
& 13
\end{aligned}
$$

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> $x+18 \quad-18+5$

$$
\begin{aligned}
& \text { +17-4 }
\end{aligned}
$$

4
$c_{0}$, at other points along the $x$-axis is also needed. For each of the 10 runs the known concentrations were plotted on $\log -\log$ paper and $c_{0}$ for each value of $x$ in the range 50 to 200 meters was determined.

Under extremely stable conditions the cloud, as might have been predicted, showed limited spreading and very little could be deduced as to the relationship of $\sqrt{y} y$ to $x$ and $y$. In unstable conditions, the cloud spread rapidly vertically and laterally. Results of the calculations are shown in the Appendix.

In Sutton's hypothesis, a cloud with its maximum concentration along the mean wind axis was assumed to be symmetrical. It was found, in practice, that the cloud was asymmetrical, and that maximum concentraction did not quite coincide with the direction of the maximum wind frequency. The $x$-axis was therefore assumed to be along the line of maximum concentration. There were also other directions along which the concentrations reached secondary maxima, with rather closely associated secondary maxima of wind frequency direction. These distributions represented superimposed bimodal or trimodal Gaussian distributions. The variance $\sqrt{y}$ of the Sutton theory was assumed, however, to be that of a unimodal Gaussian distribution, Eq. (2), but actually varied markedly from one side of the major axis of the cloud to the other, and increased also with the length of the averaging time.

There was, in most instances, a rapid decrease of $\sigma_{y}$ near the axis. For a possible explanation, let us examine the equation:

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For points near the axis, that is, for \(c_{1}\) very nearly equal to \(c_{0}\), the ratio \(c_{0} / c_{1}\) approaches one. The natural \(\log\) of one is zero, and values of the \(\log\) function near one are very small. The concentration \(c_{1}\) near the axis does not decrease rapidly at first as y increases; however y increases to the second power and the value of \(\sqrt{y}\) increases very rapidly. At a short distance from the axis the concentration \(c_{1}\) begins to decrease appreciably and the value of \(\sqrt{y}\) then begins to decrease with an increase in \(y\). This peaking of \(\sqrt{y}\) also happens to some extent as secondary maxima concen-tration-directions are sampled.

Noting that there was a straight-line decrease in \(\sqrt{y}\) with a decrease of \(x\), when these coordinates were plotted on log-log paper, for impinges well-removed from concentration maxima, an empirical relationship between \(\sigma_{y}\) and \(x^{b} y m\) was sought. The following relationship was tested:
(7) \(\sqrt{y}=D x^{b} y^{m}\)
where \(D, m\) and \(b\) are unknowns. The results from use of Eq. (7) indicated that both m and b were negative. However, observationally b should be positive when x is varied, while keeping y constant. Hence the assumed dependence upon y was rejected.

The equation was modified to the following form:
(8) \(V_{y}=B x^{b}\)

In order to get a good fit for \(b\) in each run, the statistical method of least squares was used.

Eq. (8) was reduced to the following form:

(9) \(\log \sigma_{y}=\log B+b \log x\)

Summing up this equation into the least squares form:
\[
\sum \log \sigma_{y}=N \log B+f \sum \log x
\]
(10) \(\sum \log \sigma_{y} \log x=\log B \Sigma \log x+b \Sigma(\log x)^{2}\)
where \(N\) is the number of points for which corresponding \(\sigma_{y}\) and \(x\) are available on the measuring arc. From these equations, b and B were obtained from each ten-minute run except \#1 where the thermal stability
- prevented the cloud from spreading to any extent. These values are prosented together with those of \(\sigma_{\mathbf{A}}, S R\) and \(p\) (the last two of these parameters will be defined on page 10 in Table 1.
\begin{tabular}{rlllll} 
Run & B & b & TA & SR & p \\
2 & .0276 & 1.550 & 16.5 & .0243 & .204 \\
3 & 2.9800 & 0.340 & 12.9 & .0035 & .0867 \\
4 & 1.5600 & 0.873 & 16.7 & .0118 & .128 \\
5 & 4.4500 & 0.180 & 9.2 & .0057 & .058 \\
6 & 4.3600 & 0.656 & 10.4 & .0407 & .197 \\
7 & .4170 & 0.832 & 13.5 & .0159 & .137 \\
8 & \(4.32 \times 10^{-6} 2.50\) & 12.8 & .0072 & .153 \\
9 & \(8.17 \times 10^{-7} 3.01\) & 13.1 & .0048 & .070 \\
10 & .0010 & 2.35 & 20.7 & .0048 & .099
\end{tabular}

Table 1. Values of B and b and micrometeorological parameters. The values of \(\sigma_{A}\) which appear in Table 1 wereobtained from \(\angle 2 \overline{/}\). The stability ratio, SR , was defined from the equation:
(11) \(S R=\frac{\left(T_{12}-T_{1.5}\right)+\left(Z_{12}-Z_{1.5}\right) \gamma_{d}}{u_{2}^{2}}\)
which is essentially a measure of the Richardson number. The profile contour number \(p\), which was also used extensively in the Sutton theory, is defined by the equation:
\[
\begin{equation*}
u=\mu_{1}\left(z / z_{1}\right)^{p} \tag{12}
\end{equation*}
\]

Values of winds at 12 and 6 meters from reference \(\angle 2 \overline{]}\) were used in computing p .
4. The correlation analysis.

The parameters B and b which specify \(\sqrt{V}\) were linearly correlated with each of \(T_{A}, S R\) and \(p\). The number of independent cases in each sample was \(\mathrm{N}=9\). The results of the correlation were as follows:
\[
\begin{aligned}
& 1 \mathrm{r}\left(\mathrm{~B}, \mathrm{~V}_{A}\right)=-.457 \\
& 2 \mathrm{r}\left(\mathrm{~b}, \mathrm{\sigma}_{\mathrm{A}}\right)=-.844 \\
& 3 \mathrm{r}(\mathrm{~B}, \mathrm{SR})=-.207 \\
& 4 \mathrm{r}(\mathrm{~b}, \mathrm{SR})=-.0946 \\
& 5 \mathrm{r}(\mathrm{~B}, \mathrm{p})=-.421 \\
& 6 \cdot \mathrm{r}(\mathrm{~b}, \mathrm{p})=-.601
\end{aligned}
\]

The minimum correlation coefficient which is significant at the .05 level, based on nine independent cases is .816 ; at the .10 level, the minimum is .796 .

Correlation (2) is significant at the .05 level.
Correlations (1), (5) and (6) may be significant but not at the levels of .05 or .1. The others were not significant at all.


It can be concluded that it may be possible to specify \(\sqrt{y}=\mathrm{Bx}\) b on the basis of the micrometeorological parameters \(\mathbb{V}_{A}\) and \(p\) although a larger sample of diffusion data would be necessary to establish adequate significance levels.
5. Suggestions for future research.

One of the assumptions made was that \(\sqrt{y}\) did not vary appreciably over a lateral cross-section (at fixed \(x\) ) through the cloud. The value obtained using this assumption was therefore a first approximation. It was found that the values thus obtained did vary laterally especially on passing through a secondary maximum of concentration. It would be desirable to determine values of \(\sqrt{y}\) which are relatively constant with \(y\) in spite of secondary maxima of wind frequencies.

The data for this experiment can also be analyzed for \(\sqrt{Z}\) Making the assumption, again, that \(\sqrt{y}\) and \(\sqrt{z}\) do not vary appreciably in the measuring range lateral to the axis, the following equation was derived in the same manner as the equation for \(\sqrt{y} y\), using the levels of 1.5 and 2.5 meters for which data are available:
(12) \(\frac{c_{2.5}}{c_{1.5}}=\)


If
\[
A=\exp \frac{-1.0}{2 \sqrt{z}^{2}}
\]
the resultant equation is:

(13) \(\frac{C_{2.5}}{C_{1.5}}=\frac{A+A^{16}}{1+A^{9}}\)

From this equation, A may be found, and from that \(\sqrt{\sqrt{z}}\)
In order to establish firmer tests of correlation significance, a greater number of runs should be analyzed using Eq. (8).

It is also desirable to test the diffusion model of Cramer et al \(\overline{\angle 2}\) in order to see if their diffusion parameters are more nearly predictable from the meteorological variables than of this study.
1. Barad, M. L. and Haugen, D.A., A Preliminary Analysis of Sutton \({ }^{\text { }}\) Hypothesis for a Continuous Point Source, J. Meteor., 16, pp 12-20. Feb. 1957.
2. Cramer, H.E., Record, F.A., and Vaughan, H.C., The Study of the Diffusion of Gases or Aerosols in the Lower Atmosphere. Final Report under Contract No. AF 19(604-1058, Massachusetts Institute of Technology, 1958.
3. Sutton, O.G., Micrometeorology, McGraw-Hill Book Co., Inc. 1957.


\section*{APPENDIX}

Right side-10 minutes Run 1-100 meters
\begin{tabular}{|c|c|c|c|c|}
\hline x & y & \(c_{1}\left(\mathrm{mg} / \mathrm{m}^{3}\right)\) & \(c_{0}\left(\mathrm{mg} / \mathrm{m}^{3}\right)\) & \(\sqrt{y}\) \\
\hline 93.86 & 5.23 & 190.00 & 285 & 6.79 \\
\hline 99.45 & 10.45 & 53.90 & 285 & 5.73 \\
\hline 98.77 & 15.64 & 6.15 & 286 & 5.41 \\
\hline 97.82 & 20.29 & 0.752 & 288 & 7.50 \\
\hline 96.59 & 25.88 & 0.106 & 290 & 9.17 \\
\hline \multicolumn{5}{|c|}{Run 1 - 200 meters} \\
\hline 199.7 & 10.5 & 54.9 & 117.5 & 8.53 \\
\hline 198.9 & 20.9 & 5.96 & 118. & 8.55 \\
\hline 197.5 & 31.3 & 0.231 & 119. & 8.85 \\
\hline
\end{tabular}

Run 2 - 100 meters
\begin{tabular}{lllll}
99.86 & 5.23 & 22.5 & 23.0 & 32.3 \\
99.45 & 10.45 & 22.1 & 23.3 & 33.5 \\
98.77 & 15.64 & 20.5 & 23.6 & 28.3 \\
97.82 & 20.29 & 18.6 & 23.8 & 28.8 \\
96.59 & 25.88 & 19.9 & 24.0 & 43.0 \\
95.11 & 30.90 & 12.1 & 24.2 & 26.3 \\
93.36 & 35.84 & 9.50 & 24.6 & 26.0 \\
91.36 & 40.67 & 7.53 & 24.0 & 26.4 \\
89.10 & 45.40 & 4.53 & 25.5 & 24.4 \\
86.60 & 50.00 & 1.89 & 26.0 & 21.8
\end{tabular}

Right side-10 minutes
Run 2 - 100 meters (continued)
\begin{tabular}{lllll}
\(x\) & \(y\) & \(c_{l}\) & \(c_{o}\) & \(T_{y}\) \\
83.87 & 54.46 & 1.87 & 26.8 & 23.8 \\
80.90 & 58.78 & 1.73 & 27.5 & 25.0 \\
77.72 & 62.93 & 2.49 & 28.5 & 28.5 \\
74.31 & 66.91 & 2.10 & 29.7 & 29.1 \\
70.71 & 70.71 & 0.465 & 31.0 & 24.4 \\
66.91 & 74.31 & 0.134 & 32.0 & 22.4 \\
62.93 & 77.72 & 0.46 & 34.0 & 21.4
\end{tabular}

Run 2 - 200 meters
\begin{tabular}{|c|c|c|c|c|}
\hline 199.7 & 10.5 & 5.50 & 5.75 & 18.7 \\
\hline 198.9 & 20.9 & 5.74 & 5.82 & 33.0 \\
\hline 197.5 & 31.3 & 5.68 & 5.83 & 40.3 \\
\hline 195.6 & 41.6 & 4.69 & 5.90 & 61.1 \\
\hline 193.2 & 51.8 & 3.59 & 6.00 & 52.1 \\
\hline 190.2 & 61.6 & 1.92 & 6.10 & 40.6 \\
\hline 186.7 & 71.7 & 2.28 & 6.30 & 50.3 \\
\hline 182.7 & 81.3 & 1.66 & 6.42 & 49.3 \\
\hline 178.2 & 90.8 & 1.07 & 6.60 & 47.6 \\
\hline 173.2 & 100.0 & 1.26 & 6.80 & 54.4 \\
\hline 167.7 & 108.9 & 0.841 & 7.20 & 52.4 \\
\hline 161.8 & 117.6 & 0.491 & 7.60 & 50.2 \\
\hline 155.4 & 125.9 & 0.301 & 7.82 & 49.3 \\
\hline
\end{tabular}
Pl=

\section*{Right side - 10 minutes}
\[
\text { Run } 2-200 \text { meters (continued) }
\]
\begin{tabular}{lllll}
\(x\) & \(y\) & \(c_{1}\) & \(c_{o}\) & \(\sqrt{y}\) \\
148.6 & 133.8 & 0.079 & 8.60 & 43.8
\end{tabular}

Run 3-100 meters
\begin{tabular}{lllll}
99.86 & 5.23 & 59.1 & 73.9 & 9.21 \\
99.45 & 10.45 & 44.8 & 74.5 & 10.3 \\
98.77 & 15.64 & 25.4 & 75.0 & 10.2 \\
97.82 & 20.29 & 13.3 & 75.5 & 10.8 \\
96.59 & 25.88 & 3.84 & 76.0 & 10.5 \\
95.11 & 30.90 & 0.509 & 77.0 & 13.2 \\
93.36 & 35.84 & 0.179 & 78.0 & 10.2 \\
91.37 & 45.40 & 0.061 & 79.0 & 10.7 \\
89.10 & 35.84 & 0.203 & 78.0 & 10.3
\end{tabular}

Run 3-200 meters
\begin{tabular}{lllll}
199.7 & 10.5 & 20.1 & 22.5 & 22.0 \\
198.9 & 20.9 & 10.3 & 22.7 & 16.9 \\
197.5 & 31.3 & 3.24 & 23.0 & 15.7 \\
195.6 & 41.6 & 0.855 & 23.5 & 16.5 \\
193.2 & 51.8 & 0.102 & 24.0 & 15.7
\end{tabular}

Run 4 - 100 meters
\begin{tabular}{lrlll}
99.96 & 5.23 & 52.2 & 55.0 & 19.8 \\
99.45 & 10.45 & 42.5 & 55.3 & 14.6 \\
98.77 & 15.64 & 30.3 & 55.7 & 13.6
\end{tabular}


\section*{Right side - 10 minutes}

Run 4-100 meters (continued)
\begin{tabular}{|c|c|c|c|c|}
\hline X & Y & \({ }^{\text {c }}\) & \({ }^{\circ}\) & \(\sqrt{y}\) \\
\hline 97.82 & 20.29 & 24.5 & 56.0 & 15.8 \\
\hline 96.59 & 25.88 & 20.2 & 56.5 & 18.2 \\
\hline 95.11 & 30.90 & 22.3 & 57.0 & 22.8 \\
\hline 93.36 & 35.84 & 22.8 & 57.5 & 26.5 \\
\hline 91.36 & 40.67 & 21.5 & 58.0 & 29.7 \\
\hline 89.10 & 45.40 & 17.6 & 59.0 & 29.3 \\
\hline 86.60 & 50.00 & 14.2 & 60.0 & 29.5 \\
\hline 83.87 & 54.46 & 16.5 & 61.0 & 33.8 \\
\hline 80.90 & 58.78 & 6.86 & 62.0 & 28.3 \\
\hline 77.72 & 62.93 & 4.25 & 63.0 & 27.2 \\
\hline 74.31 & 66.91 & 3.63 & 65.0 & 28.3 \\
\hline 70.71 & 70.71 & 2.30 & 66.0 & 27.4 \\
\hline 66.91 & 74.31 & 1.16 & 69.0 & 26.1 \\
\hline 62.93 & 77.72 & 1.37 & 71.0 & 27.5 \\
\hline 58.78 & 80.90 & 0.344 & 73.0 & 24.8 \\
\hline 54.46 & 83.87 & 0.053 & 77.0 & 26.6 \\
\hline \multicolumn{5}{|c|}{Run 4 - 200 meters} \\
\hline 199.7 & 10.5 & 12.8 & 14.2 & 23.0 \\
\hline 198.9 & 20.9 & 11.3 & 14.3 & 30.2 \\
\hline 197.5 & 31.3 & 10.4 & 14.4 & 38.5 \\
\hline 195.6 & 41.6 & 8.2 & 14.5 & 38.7 \\
\hline
\end{tabular}


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\section*{\(\square\)}

8 13 1 \(+\square\) \(1=1\) 5 \(=-x\)
\(y=2\) \(=-\) 5



\section*{Right side - 10 minutes}

Run 4 - 200 meters (continued)
\begin{tabular}{lllll}
x & y & \(c_{1}\) & \(c_{0}\) & \(\mathrm{\sigma y}\) \\
193.2 & 51.8 & 4.96 & 14.8 & 35.0 \\
190.2 & 61.6 & 5.58 & 15.0 & 43.9 \\
186.7 & 71.7 & 4.96 & 15.4 & 47.6 \\
182.7 & 81.3 & 4.41 & 15.8 & 50.7 \\
178.2 & 90.8 & 3.84 & 16.2 & 53.9 \\
173.2 & 100.0 & 3.05 & 16.5 & 54.4 \\
167.7 & 117.6 & 2.69 & 17.3 & 55.3 \\
161.8 & 125.9 & 0.950 & 20.3 & 57.0 \\
155.4 & 133.8 & 0.610 & 22.0 & 50.7 \\
148.6 & 141.4 & 0.410 & 24.0 & 49.7 \\
141.4 & 148.6 & 0.197 & 27.0 & 47.2 \\
133.8 & & & & \\
\hline
\end{tabular}

\section*{Run 5 - 100 meters}
\begin{tabular}{lllll}
99.86 & 5.23 & 256 & 284 & 13.5 \\
99.45 & 10.45 & 209 & 286 & 12.2 \\
98.77 & 15.64 & 70.8 & 288 & 8.92 \\
97.82 & 20.29 & 19.8 & 290 & 8.75 \\
96.59 & 25.88 & 2.47 & 295 & 8.35 \\
95.11 & 30.90 & 0.671 & 300 & 8.83 \\
93.36 & 35.84 & 0.239 & 310 & 9.43 \\
91.38 & 40.67 & 0.160 & 320 & 10.4
\end{tabular}

\section*{Right side - 10 minutes}

Run 5 - 100 meters (continued)
\begin{tabular}{lcccc}
\(x\) & \(y\) & \(c_{1}\) & \(c_{0}\) & \(\Gamma_{y}\) \\
89.10 & 45.40 & 0.166 & 330 & 11.6 \\
& Run \(5-200\) meters & & \\
199.7 & 10.5 & 75.5 & 137. & 9.60 \\
198.9 & 20.9 & 30.8 & 137 \\
197.5 & 31.3 & 2.24 & 137. & 12.1 \\
195.6 & 41.6 & 0.344 & 137. & 12.0
\end{tabular}

\section*{Run 6 - 100 meters}
\begin{tabular}{lcccc}
99.86 & 5.23 & 79.7 & 89.9 & 12.5 \\
99.45 & 10.45 & 64.3 & 89.9 & 12.6 \\
98.77 & 15.64 & 55.3 & 90.0 & 14.2 \\
97.82 & 20.29 & 50.7 & 91.0 & 18.7 \\
96.59 & 25.88 & 38.5 & 91.5 & 19.6 \\
95.11 & 30.90 & 20.1 & 92.0 & 17.2 \\
93.36 & 35.84 & 8.79 & 93.0 & 16.4 \\
91.36 & 40.67 & 1.64 & 93.5 & 14.2 \\
89.10 & 45.40 & 0.102 & 94.5 & 12.2
\end{tabular}

Run 6 - 200 meters
\begin{tabular}{lllll}
199.7 & 10.5 & 20.5 & 28.4 & 12.5 \\
198.9 & 20.9 & 16.1 & 28.4 & 19.7 \\
197.5 & 31.3 & 14.5 & 28.4 & 27.9 \\
195.6 & 41.6 & 11.8 & 28.8 & 31.1
\end{tabular}
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Right side - 10 minutes
Run 6 - 200 meters (continued)
\begin{tabular}{lllll}
\(x\) & \(y\) & \(c_{1}\) & \(c_{0}\) & Ty \\
190.2 & 61.6 & 8.43 & 29.3 & 32.7 \\
186.7 & 71.7 & 0.662 & 30.0 & 25.8 \\
182.7 & 81.3 & 0.200 & 31.0 & 25.5
\end{tabular}

Run 7 - 100 meters
\begin{tabular}{lllll}
99.86 & 5.23 & 35.8 & 39.9 & 13.8 \\
99.45 & 10.45 & 35.3 & 39.9 & 21.3 \\
98.77 & 15.64 & 34.8 & 39.9 & 29.4 \\
97.82 & 20.29 & 26.1 & 40.0 & 22.0 \\
96.59 & 25.88 & 15.4 & 41.0 & 18.5 \\
95.11 & 30.90 & 8.05 & 41.2 & 16.8 \\
93.36 & 35.84 & 4.66 & 41.5 & 17.1 \\
91.36 & 40.67 & 2.21 & 41.8 & 16.8 \\
89.10 & 45.40 & 0.500 & 42.3 & 15.2 \\
86.60 & 50.00 & 0.065 & 43.0 & 13.8
\end{tabular}

Run 7 - 200 meters
\begin{tabular}{lllll}
199.7 & 10.5 & 12.0 & 13.7 & 20.6 \\
198.9 & 20.9 & 8.38 & 13.8 & 20.9 \\
197.5 & 31.6 & 5.41 & 14.0 & 22.5 \\
195.6 & 41.6 & 3.00 & 14.2 & 23.6 \\
193.2 & 51.8 & 1.33 & 14.5 & 23.7 \\
190.2 & 61.6 & 0.615 & 15.0 & 24.4 \\
186.7 & 71.7 & 0.239 & 15.7 & 24.8
\end{tabular}


Right side - 10 minutes
Run 8 - 100 meters
\begin{tabular}{lllll}
x & y & \(c_{1}\) & \(c_{0}\) & \(\sigma_{y}\) \\
99.86 & 5.23 & 47.7 & 49.7 & 21.9 \\
99.45 & 10.45 & 34.4 & 49.7 & 13.1 \\
98.77 & 15.64 & 20.5 & 29.7 & 11.3 \\
97.82 & 20.24 & 8.14 & 49.7 & 10.6 \\
96.59 & 25.88 & 1.55 & 50.3 & 9.8 \\
95.11 & 30.90 & 0.410 & 51.5 & 9.9 \\
93.36 & 35.84 & 0.109 & 51.8 & 10.2
\end{tabular}

Run 8 - 200 meters
\begin{tabular}{lllll}
199.7 & 10.5 & 11.9 & 14.1 & 18.8 \\
198.9 & 20.9 & 7.38 & 14.1 & 18.4 \\
197.5 & 31.3 & 2.72 & 14.2 & 20.6 \\
195.6 & 41.6 & 0.936 & 14.3 & 17.9 \\
193.2 & 51.8 & 0.207 & 14.7 & 17.7
\end{tabular}

\section*{Run 9 - 100 meters}
\begin{tabular}{lllll}
99.86 & 5.23 & 51.1 & 59.2 & 11.2 \\
99.45 & 10.45 & 47.7 & 59.2 & 15.9 \\
98.77 & 15.64 & 40.4 & 59.2 & 17.1 \\
97.82 & 20.29 & 38.2 & 59.2 & 21.6 \\
96.82 & 25.88 & 23.9 & 59.8 & 19.2 \\
95.11 & 30.90 & 12.4 & 60.0 & 17.4 \\
93.36 & 35.84 & 6.73 & 62.0 & 20.2
\end{tabular}


\section*{Right side - 10 minutes}

Run 9 - 100 meters (continued)
\begin{tabular}{lllll}
\(x\) & \(y\) & \(c_{1}\) & \(c_{0}\) & \(\sqrt{y y}\) \\
91.36 & 40.67 & 2.92 & 64.0 & 16.4 \\
89.10 & 45.40 & 0.686 & 65.0 & 15.0 \\
86.60 & 50.00 & 0.127 & 75.0 & 14.0
\end{tabular}

Run 9 - 200 meters
\begin{tabular}{lllll}
199.7 & 10.5 & 16.6 & 17.4 & 33.4 \\
198.9 & 20.9 & 14.3 & 17.4 & 33.0 \\
197.5 & 31.3 & 11.2 & 17.7 & 34.3 \\
195.6 & 41.6 & 5.79 & 18.0 & 27.6 \\
193.2 & 51.8 & 4.67 & 18.5 & 31.3 \\
190.2 & 61.6 & 3.27 & 18.9 & 33.0 \\
186.7 & 71.7 & 0.480 & 19.7 & 26.3
\end{tabular}

Run 10 - 100 meters
\begin{tabular}{lllll}
99.86 & 5.23 & 24.8 & 28.4 & 11.6 \\
99.45 & 10.45 & 20.2 & 28.4 & 12.6 \\
98.77 & 15.64 & 16.1 & 29.0 & 14.4 \\
97.82 & 20.29 & 16.0 & 29.5 & 18.4 \\
96.59 & 25.88 & 13.8 & 30.2 & 21.4 \\
95.11 & 30.90 & 14.4 & 32.0 & 24.8 \\
93.36 & 35.84 & 20.2 & 33.5 & 28.3 \\
91.36 & 40.67 & 24.2 & 37.2 & 43.9 \\
89.10 & 45.40 & 19.0 & 39.0 & 37.8 \\
86.60 & 50.00 & 16.6 & 39.7 & 37.9
\end{tabular}


Run 10 - 100 meters (continued)
\begin{tabular}{lllll}
x & y & \(c_{1}\) & \(c_{0}\) & Jy \\
83.87 & 54.46 & 14.2 & 45.3 & 35.8 \\
80.90 & 58.78 & 10.3 & 47.5 & 33.6 \\
77.72 & 62.93 & 4.87 & 49.2 & 29.3 \\
74.31 & 66.91 & 2.19 & 50.1 & 26.7 \\
70.71 & 70.71 & 1.94 & 58.0 & 27.1 \\
66.91 & 74.31 & 2.86 & 67.0 & 29.6 \\
62.93 & 77.72 & 4.72 & 78.0 & 26.6 \\
58.78 & 80.90 & 3.50 & 87.0 & 32.3
\end{tabular}

Run 10 - 200 meters
\begin{tabular}{|c|c|c|c|c|}
\hline 199.7 & 10.5 & 3.03 & 4.71 & 11.2 \\
\hline 198.9 & 20.9 & 3.79 & 4.71 & 31.8 \\
\hline 197.5 & 31.3 & 4.26 & 4.9 & 59.1 \\
\hline 195.6 & 4.6 & 3.23 & 5.0 & 44.2 \\
\hline 193.2 & 51.8 & 2.92 & 5.1 & 48.9 \\
\hline 190.2 & 61.6 & 1.46 & 5.2 & 45.0 \\
\hline 186.7 & 71.7 & 1.00 & 5.3 & 39.2 \\
\hline 182.7 & 81.3 & 1.43 & 5.4 & 49.6 \\
\hline 178.2 & 90.8 & 2.79 & 5.6 & 76.5 \\
\hline 173.2 & 100.0 & 3.49 & 6.1 & 94.4 \\
\hline 167.7 & 108.9 & 2.41 & 6.8 & 75.5 \\
\hline 161.8 & 117.6 & 3.11 & 7.2 & 90.2 \\
\hline
\end{tabular}

Right side - 10 minutes
Run 10 - 200 meters (continued)
\begin{tabular}{lllll}
x & y & 61 & \(c o\) & \(\mathrm{~T} y\) \\
155.4 & 125.9 & 2.78 & 8.3 & 85.0 \\
148.6 & 133.8 & 1.05 & 9.5 & 63.8 \\
141.4 & 141.4 & 0.597 & 10.0 & 58.6 \\
133.8 & 148.6 & 0.527 & 11.0 & 60.3 \\
125.9 & 155.4 & 0.967 & 13.0 & 68.6 \\
117.6 & 161.8 & 1.17 & 17.0 & 69.7 \\
108.9 & 167.7 & 0.166 & 19.0 & 54.7
\end{tabular}



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